**Laboratory work 8**

**Development of tracking filter of a moving object   
when measurements and motion model are in different coordinate systems**

Performance - Tuesday, April 26, 2016

Due to submit a performance report – TBD

The objective of this laboratory work is to develop a tracking filter of a moving object   
when measurements and motion model are in different coordinate systems. This problem is typical for radio navigation systems. Important outcome of this exercise is to detect main difficulties of practical Kalman filter implementation related with instability zone of a tracking filter, and to analyze conditions under which navigation system may become blind and filter diverges. Additional important outcome of this exercise is experience in developing algorithms to improve tracking accuracy of a moving object by taking into account available a prior information. This is important to prevent collisions and for other safety issues.

The first part of this laboratory work is performed in the class by students as in teams of 2 on April 26, 2016 and the team will submit one document reporting about the performance till TBD. Within your group, you may discuss all issues openly, and discuss and debate until you reach a consensus.

*Important information*

Please read charts for problem formulation

**Tracking\_filter\_cordinate\_transformation\_of\_measurements\_April\_22\_2016.pdf**

This laboratory work consists of two parts:

1. Instability zone of a tracking filter due to ill-conditioned coordinate transformations   
   of measurements (Tuesday, April 26, 2016.
2. How to increase tracking accuracy of a moving object by taking into account available a prior information? (Thursday, April 28, 2016)

***Here is the recommended procedure for part I:***

***Instability zone of a tracking filter due to ill-conditioned coordinate transformations   
of measurements.***

1. Generate a true trajectory of an object that moves uniformly. Trajectory is deterministic, as no random disturbance affect a motion.

Cartesian coordinates and components of velocity and are determined by

***Initial conditions to generate trajectory***

1. Size of trajectory is points.
2. – interval between measurements.
3. Initial components of velocity

It means that an object moves toward an observer.

1. Initial coordinates

This means that an object starts it motion **at a quite great distance from an observer**.

Later we will analyze when an object starts its motion **at a quite close distance from an  
observer.**

1. Generate also true values of range and azimuth

Initial values ;

Plot generated motion in polar coordinate system.

You can use command polarplot()

1. Generate measurements and of range and azimuth

Variances of measurement noises are given by

Later we will analyze other conditions.

1. Transform polar coordinates and to Cartesian ones and get pseudo-measurements   
   of coordinates and

Consult charts, page 31

1. Create the measurement vector from pseudo-measurements of coordinates and   
   Consult charts, page 31
2. Initial conditions for Kalman filter algorithm  
   Initial filtered estimate of state vector

Initial filtration error covariance matrix

1. Create the transition matrix and observation matrix

Consult charts, page 32

1. Create the measurement error covariance matrix needed for Kalman filter algorithm

Consult charts, page 33

1. Develop Kalman filter algorithm to estimate state vector (extrapolation and filtration)

At every extrapolation and filtration step you will need to calculate range and azimuth from extrapolated and filtered estimates.

1. Run Kalman filter algorithm over runs.

Calculate true errors of estimation:

1. Errors of extrapolation and filtration estimates of range .
2. Errors of extrapolation and filtration estimates of azimuth .

Make conclusions if these errors decrease or increase with time.

1. Analyze dependence of coordinate on azimuth

According to coordinate transformation and has nonlinear relation

Plot dependence of coordinate on azimuth .

Is it really nonlinear in these conditions?

Or it is close to linear?

If this dependence is close to linear it means that linearization errors are insignificant.

1. Calculate condition number of covariance matrix over the observation interval.

Does condition number decrease or increase over time?

If condition number close to 1, than matrix is well-conditioned.

If condition number is relatively great, then matrix is ill-conditioned.

1. Analyze filter gain . Dimension of filter gain in this case is .

Plot . Note that values of over observation interval don’t always belong to interval (0,1) .This is related to the fact that matrix depends on polar measurements that have errors. Ways to adjust filter gain to be in the required range (0,1) can be analyzed, but this is not the goal of current assignment.

1. Run filter again over runs but use other initial conditions to generate a trajectory

This means that an object starts it motion **at a quite close distance from an observer**.

Check by plotting new polar coordinates.

1. Calculate true errors of estimation:
2. Errors of extrapolation and filtration estimates of range
3. Errors of extrapolation and filtration estimates of azimuth .

Make conclusions if these errors decrease or increase with time.

1. Analyze dependence of coordinate on azimuth by plotting   
   Is it nonlinear or linear in these conditions?

Linearization errors are significant or insignificant?

1. Calculate condition number of covariance matrix over the observation interval for these conditions. Does condition number decrease or increase over time?
2. Make conclusions how linearization errors affect tracking accuracy and how important for tracking accuracy is starting position of a moving object (close or far from an observer).
3. Run filter again over runs. Use again initial conditions to generate a trajectory

This means that an object starts it motion **at a quite close distance from an observer**.

But to generate polar measurements and (item 3) use other values of variances

of measurement noises :

1. Repeat items 14,15,16,17 for these conditions and reply to questions addressed.
2. Make final conclusions under which conditions navigation system becomes blind and filter diverges. Which factors has the greatest influence? Linearization errors or ill-conditioned problem? Which solution can help to overcome this particular ill-conditioned problem?

***Performance report***

1. Performance report should contain all the items listed
2. The code should be commented. It should include:

* Title of the laboratory work, for example

% Converting a physical distance to a grid distance using least-square method

* The names of a team, indication of Skoltech, and date, for example,   
  %Tatiana Podladchikova, Skoltech, 2016

Main procedures also should be commented, for example

%13-month running mean

…here comes the code

1. If your report includes a plot, then it should contain: title, title of x axis, title of y axis, legend of lines on plot.